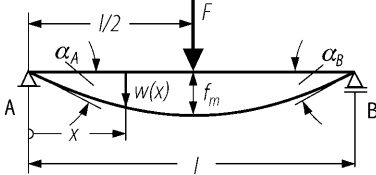
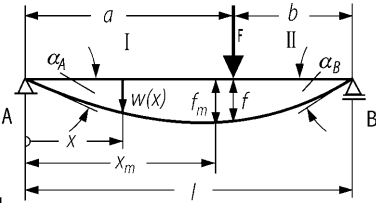
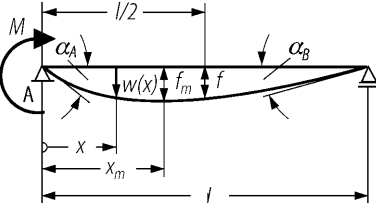
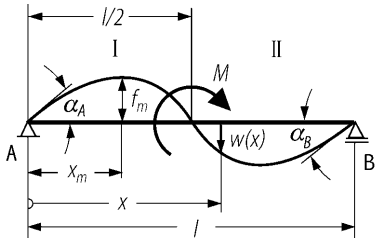
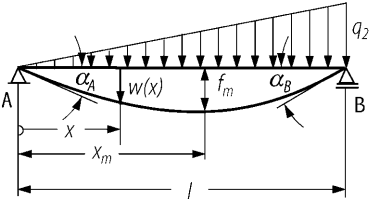
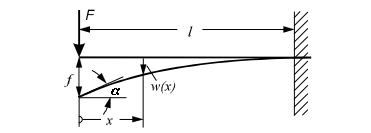
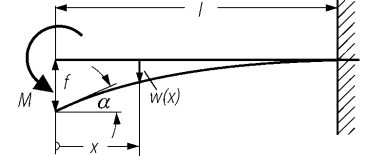
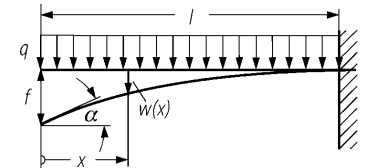
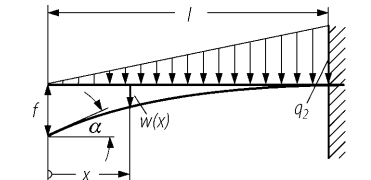
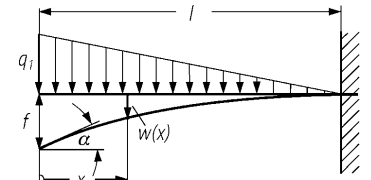
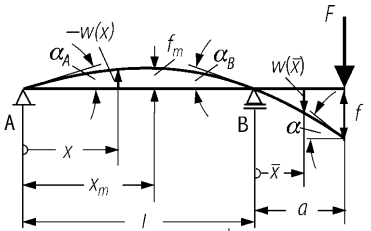
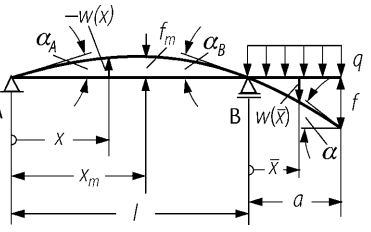


Tabelle 5a. Biegelinien von statisch bestimmten Trägern mit konstantem Querschnitt

	Belastungsfall	Gleichung der Biegelinie	Durchbiegung	Neigungswinkel
1		$0 \leq x \leq l/2 :$ $w(x) = \frac{Fl^3}{48EI_y} \left[3\frac{x}{l} - 4\left(\frac{x}{l}\right)^3 \right]$	$f_m = \frac{Fl^3}{48EI_y}$	$\alpha_A = \alpha_B = \frac{Fl^2}{16EI_y}$
2		$0 \leq x \leq a :$ $w_I(x) = \frac{Fab^2}{6EI_y} \left[\left(1 + \frac{l}{b}\right)\frac{x}{l} - \frac{x^3}{abl} \right]$ $a \leq x \leq l :$ $w_{II}(x) = \frac{Fa^2b}{6EI_y} \left[\left(1 + \frac{l}{a}\right)\frac{l-x}{l} - \frac{(l-x)^3}{abl} \right]$	$f = \frac{Fa^2b^2}{3EI_y l}$ $a > b : f_m = \frac{Fb\sqrt{(l^2 - b^2)^3}}{9\sqrt{3}EI_y l}$ in $x_m = \sqrt{(l^2 - b^2)}/3$ $a < b : f_m = \frac{Fa\sqrt{(l^2 - a^2)^3}}{9\sqrt{3}EI_y l}$ in $x_m = l - \sqrt{(l^2 - a^2)}/3$	$\alpha_A = \frac{Fab(l+b)}{6EI_y l}$ $\alpha_B = \frac{Fab(l+a)}{6EI_y l}$
3a		$w(x) = \frac{Ml^2}{6EI_y} \left[2\frac{x}{l} - 3\left(\frac{x}{l}\right)^2 + \left(\frac{x}{l}\right)^3 \right]$	$f = \frac{Ml^2}{16EI_y}$ in $x = \frac{l}{2}$ $f_m = \frac{Ml^2}{9\sqrt{3}EI_y}$ in $x_m = l - \frac{l}{\sqrt{3}}$	$\alpha_A = \frac{Ml}{3EI_y}$ $\alpha_B = \frac{Ml}{6EI_y}$
3b		$0 \leq x \leq l/2 :$ $w_I = \frac{Ml^2}{24EI_y} \left[-\frac{x}{l} + 4\left(\frac{x}{l}\right)^3 \right]$ $l/2 \leq x \leq l :$ $w_{II} = \frac{Ml^2}{24EI_y} \left[-3 + 11\frac{x}{l} - 12\left(\frac{x}{l}\right)^2 + 4\left(\frac{x}{l}\right)^3 \right]$	$f_{mI} = f_{mII} = \frac{Ml^2}{72\sqrt{3}EI_y}$ in $x_{mI} = \frac{l}{2\sqrt{3}}$ bzw. in $x_{mII} = l \left(1 - \frac{1}{2\sqrt{3}}\right)$	$\alpha_A = \alpha_B = \frac{Ml}{24EI_y}$

3c		$0 \leq x \leq a:$ $w_I(x) = \frac{Ml^2}{6EI_y} \left[\left(2 - 6\frac{a}{l} + 3\frac{a^2}{l^2} \right) \frac{x}{l} + \left(\frac{x}{l} \right)^3 \right]$ $a \leq x \leq l:$ $w_{II}(x) = \frac{-Ml^2}{6EI_y} \left[3\left(\frac{a}{l} \right)^2 - \left(2 + 3\left(\frac{a}{l} \right)^2 \right) \frac{x}{l} + 3\left(\frac{x}{l} \right)^2 - \left(\frac{x}{l} \right)^3 \right]$	$a > b: \text{ in } x_m = l \sqrt{\frac{2a}{l} - \frac{2}{3} - \left(\frac{a}{l} \right)^2}$ $f_m = \frac{Ml^2}{6EI_y} \left(\left(\frac{6a}{l^2} - \frac{2}{l} - \frac{3a^2}{l^3} \right) x_m - \left(\frac{x_m}{l} \right)^3 \right)$	$\alpha_A = -\frac{Ml}{6EI_y} \left(2 - 6\frac{a}{l} + 3\left(\frac{a}{l} \right)^2 \right)$ $\alpha_B = \frac{Ml}{6EI_y} \left(1 - 3\left(\frac{a}{l} \right)^2 \right)$
3d		$w(x) = \frac{Ml^2}{6EI_y} \left[\frac{x}{l} - \left(\frac{x}{l} \right)^3 \right]$	$f = \frac{Ml^2}{16EI_y} \text{ in } x = \frac{l}{2}$ $f_m = \frac{Ml^2}{9\sqrt{3}EI_y} \text{ in } x_m = \frac{l}{\sqrt{3}}$	$\alpha_A = \frac{Ml}{6EI_y}$ $\alpha_B = \frac{Ml}{3EI_y}$
4		$w(x) = \frac{ql^4}{24EI_y} \left[\frac{x}{l} - 2\left(\frac{x}{l} \right)^3 + \left(\frac{x}{l} \right)^4 \right]$	$f_m = \frac{5}{384} \frac{ql^4}{EI_y}$	$\alpha_A = \alpha_B = \frac{ql^3}{24EI_y}$

5		$w(x) = \frac{q_2 l^4}{360 E I_y} \left[7 \frac{x}{l} - 10 \left(\frac{x}{l} \right)^3 + 3 \left(\frac{x}{l} \right)^5 \right]$	$f_m = \frac{q_2 l^4}{153,3 E I_y} \text{ in } x_m = 0,519 l$	$\alpha_A = \frac{7}{360} \frac{q_2 l^3}{E I_y}$ $\alpha_B = \frac{8}{360} \frac{q_2 l^3}{E I_y}$
6		$w(x) = \frac{F l^3}{6 E I_y} \left[2 - 3 \frac{x}{l} + \left(\frac{x}{l} \right)^3 \right]$	$f = \frac{F l^3}{3 E I_y}$	$\alpha = \frac{F l^2}{2 E I_y}$
7		$w(x) = \frac{M l^2}{2 E I_y} \left[1 - 2 \frac{x}{l} + \left(\frac{x}{l} \right)^2 \right]$	$f = \frac{M l^2}{2 E I_y}$	$\alpha = \frac{M l}{E I_y}$
8		$w(x) = \frac{q l^4}{24 E I_y} \left[3 - 4 \frac{x}{l} + \left(\frac{x}{l} \right)^4 \right]$	$f = \frac{q l^4}{8 E I_y}$	$\alpha = \frac{q l^3}{6 E I_y}$
9		$w(x) = \frac{q_2 l^4}{120 E I_y} \left[4 - 5 \frac{x}{l} + \left(\frac{x}{l} \right)^5 \right]$	$f = \frac{q_2 l^4}{30 E I_y}$	$\alpha = \frac{q_2 l^3}{24 E I_y}$
10		$w(x) = \frac{q_1 l^4}{120 E I_y} \left[11 - 15 \frac{x}{l} + 5 \left(\frac{x}{l} \right)^4 - \left(\frac{x}{l} \right)^5 \right]$	$f = \frac{11}{120} \frac{q_1 l^4}{E I_y}$	$\alpha = \frac{q_1 l^3}{8 E I_y}$

11		$0 \leq x \leq l:$ $w(x) = -\frac{Fal^2}{6EI_y} \left[\frac{x}{l} - \left(\frac{x}{l} \right)^3 \right]$ $0 \leq \bar{x} \leq a:$ $w(\bar{x}) = \frac{Fa^3}{6EI_y} \left[2 \frac{l}{a} \frac{\bar{x}}{a} + 3 \left(\frac{\bar{x}}{a} \right)^2 - \left(\frac{\bar{x}}{a} \right)^3 \right]$	$f = \frac{Fa^2(l+a)}{3EI_y}$ $f_m = \frac{Fal^2}{9\sqrt{3}EI_y} \text{ in } x_m = \frac{l}{\sqrt{3}}$	$\alpha = \frac{Fa(2l+3a)}{6EI_y}$ $\alpha_A = \frac{Fal}{6EI_y}$ $\alpha_B = \frac{Fal}{3EI_y}$
12		$0 \leq x \leq l:$ $w(x) = -\frac{qa^2l^2}{12EI_y} \left[\frac{x}{l} - \left(\frac{x}{l} \right)^3 \right]$ $0 \leq \bar{x} \leq a:$ $w(\bar{x}) = \frac{qa^4}{24EI_y} \left[4 \frac{l}{a} \frac{\bar{x}}{a} + 6 \left(\frac{\bar{x}}{a} \right)^2 - 4 \left(\frac{\bar{x}}{a} \right)^3 + \left(\frac{\bar{x}}{a} \right)^4 \right]$	$f = \frac{qa^3(4l+3a)}{24EI_y}$ $f_m = \frac{qa^2l^2}{18\sqrt{3}EI_y} \text{ in } x_m = \frac{l}{\sqrt{3}}$	$\alpha = \frac{qa^2(l+a)}{6EI_y}$ $\alpha_A = \frac{qa^2l}{12EI_y}$ $\alpha_B = \frac{qa^2l}{6EI_y}$